

# Non-Linear MHD Simulation with JOREK on HELIOS-CSC

S. Pamela

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A.Fil, E.Nardon, J.Morales, A.Lessig, I.Krebs ...



HELIOS-CSC Review Meeting, 15 March 2016

# Outline

- **Presentation of the JOREK code**
  - [www.jorek.eu](http://www.jorek.eu)
  - The JOREK team
  - Eurofusion ENR project
  - Numerical details
  - The reduced-MHD model
  - Running JOREK on HELIOS-CSC
  
- **Physics Results 2015**
  - ELMs
  - RMP
  - Pellets
  - QH-mode
  - MGI disruptions
  
- **Conclusion**
  - Summary
  - Future work

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## - Physics Results 2015

ELMs

RMP

Pellets

QH-mode

MGI disruptions

## - Conclusion

Summary

Future work

## JOREK website, including

- References
- Team members
- wiki (restricted)
- Forum (restricted)

*JOREK is a non-linear extended MHD code for toroidal X-point geometries.*

### The JOREK Code

The non-linear extended MHD code JOREK resolves realistic toroidal X-point geometries with a C1 continuous flux-surface aligned grid including main plasma, scrape-off layer and divertor region. It is based on robust fully implicit numerics, and includes divertor boundary conditions, 3D resistive wall effects, two-fluid effects and neoclassical flows.

The well established physics and numerics community around JOREK has strong connections to the relevant experiments, the ITER Organization and the respective ITPA Topical Groups.

### Key Physics Applications

- Edge Localized Modes (ELMs)
- Pellet triggering of Edge Localized Modes
- Error field penetration for resonant magnetic perturbations (RMPs)
- Mitigation / suppression of ELMs via RMP fields
- Massive gas injection triggered disruptions
- Stabilization of Tearing Modes via ECCD
- Vertical Displacement Events
- Resistive Wall Modes
- QH-Mode



### Physics Models

- Reduced and full MHD models
- Two-fluid and neoclassical effects
- Divertor model
- Pellet ablation model
- Neutrals model for Deuterium MGI — impurity MGI model under development
- Resistive wall extension — inclusion of Halo currents under development
- Electron Cyclotron Current Drive (ECCD) model
- Particle in cell model under development

# The JOREK Team

> 30 members

> 10 international institutions

Includes physicists and mathematicians

Strong collaboration with PaStiX team (direct solver) [ref]

## The Present JOREK Team (alphabetical)

- Calin Atanasiu
- Marina Bécoulet
- Pavel Cahyna ([website](#))
- Celine Caldini-Queiros ([website](#))
- Jose Costa
- Guilhem Dif-Pradalier
- Elise Estibals
- Alexandre Fil ([website](#))
- Emmanuel Franck ([website](#))
- Shimpei Futatani
- Virginie Grandgirard
- Herve Guillard
- Florian Hindenlang
- Matthias Hoelzl ([website](#))
- Guido Huijsmans ([website](#))
- Xavier Lacoste
- Guillaume Latu ([website](#))
- Alexander Lessig
- Feng Liu
- Jorge Morales
- Eric Nardon
- Boniface Nkonga
- Francois Orain
- Stanislas Pamela
- Chantal Passeron
- Jane Pratt ([website](#))
- Ahmed Ratnani ([website](#))
- Afeintou Sangam
- Cristian Sommariva
- Eric Sonnendrücker ([website](#))
- Erika Strumberger
- Daan van Vugt
- Egbert Westerhof

# Eurofusion ENR Project

PI: M.Hoelzl  
 over 10 ppy ~ 450 k€ / year  
 Progress is on schedule

## 2. Project deliverables

Deliverables planned for 2015	Achieved?	Evidence // Reason for partial or non-achievement
Status report after one year	Fully	at hand
First JOREK simulation of non-deuterium massive gas injection (MGI)	Partly	Model has been derived but implementation was delayed by ~3-6 months. Reason: the following new deliverable.
Investigation of gas penetration with the IMAGINE code ( <b>New deliverable</b> )	Fully	Refereed article submitted [5]; <i>This turned out to be important to improve and validate the JOREK MGI model</i>
First JOREK simulation of a complete thermal quench ( <b>Originally planned for 6/2016</b> )	Fully	Presentations [23,24]; Publication in preparation
First JOREK simulation of an ELM cycle with a realistic bootstrap current model	Fully	First successful non-linear simulations have been carried out; publication in preparation (will take time)
First JOREK simulation of an ELM crash with high recycling divertor conditions	Partly	Model successfully implemented and tested; application to ELM simulations has been started
Analytical and numerical study of ELM precursors and filaments in rotating plasmas	Fully	Refereed article submitted [10]
Implementation of Newton iterations for the time stepping	Fully	Refereed article [8]
Study of stability and theoretical properties of reduced MHD with two-fluid effects	Fully	Report in preparation
Report on the implementation of new development workflows	Fully	Documented in jorek.eu wiki; updated through user's feedback

# Numerical Details

**Full domain with core, SOL and X-point :**

- Cubic finite-elements
- Flux-aligned poloidal grid
- Fourier series in toroidal direction

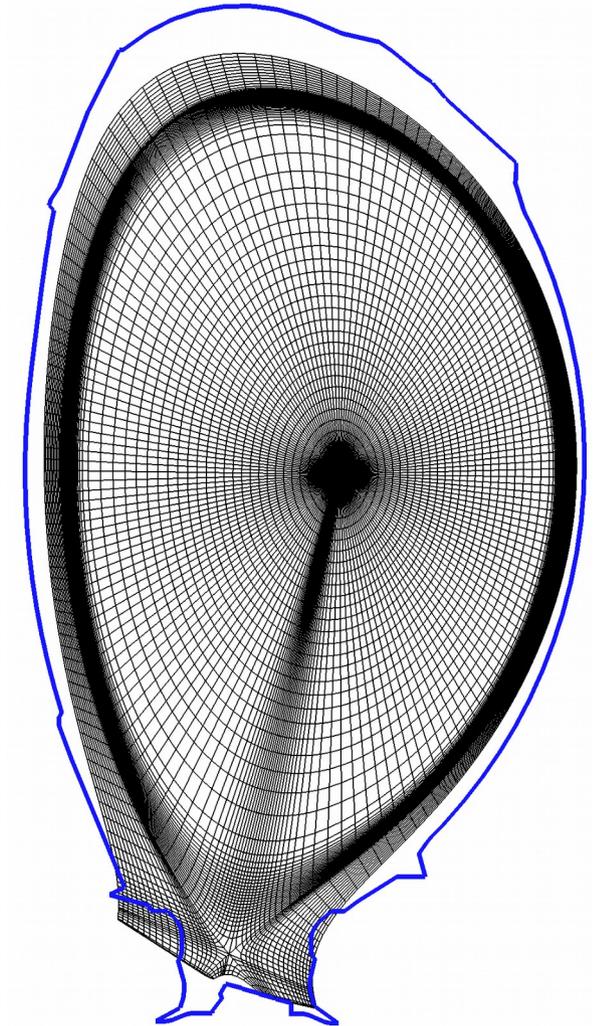
*[G.Huysmans, Nuc.Fus. 2007]*

*[O.Czarny, Journ. Comp. Phys. 2008]*

**Implicit time-stepping :**

- Crank-Nicolson & Gears schemes
- Time step depends on MHD activity only
- GMRES iterative solver
- Physical preconditioner using sub-matrices solved  
With Sparse-matrix solver PastiX

*[P.Henon, Parallel Comput. 34 (2008)]*



**JET grid**

# Reduced MHD Model

[H. Strauss, Phys. Fluids 19 134 (1976)]

$$\vec{B} = \vec{B}_\phi + \vec{B}_p = \frac{F_o}{R} \vec{e}_\phi + \frac{1}{R} \nabla \psi \times \vec{e}_\phi,$$

**perp. momentum**

$$\begin{aligned} \vec{v}_{tot} &= \vec{v}_\parallel + \vec{v}_\perp = \vec{v}_\parallel + \vec{v}_E + \vec{v}_{*i} \\ &= v_\parallel \vec{B} + R \vec{e}_\phi \times \nabla \Phi + \frac{\delta^* R}{\rho} \vec{e}_\phi \times \nabla p_i, \end{aligned}$$

$$\rho \frac{\partial \vec{v}_E}{\partial t} = - \rho \vec{v}_{*i} \cdot \nabla \vec{v}_E - \nabla_\perp p + \vec{J} \times \vec{B} + \mu \nabla^2 (\vec{v}_E + \vec{v}_{*i})$$

**par. momentum**

$$\rho \frac{\partial \vec{v}_\parallel}{\partial t} = - \rho \vec{v}_\parallel \cdot \nabla \vec{v}_\parallel - \nabla_\parallel p + \mu \nabla^2 (\vec{v}_\parallel - \vec{v}_{NBI})$$

**Ohm's law**

$$\frac{\partial \psi}{\partial t} = \eta (j - j_A) + R [\psi, \Phi] - \frac{\delta^* R}{\rho} [\psi, p] - \frac{\partial \Phi}{\partial \phi} + \frac{\delta^*}{\rho} \frac{\partial p}{\partial \phi}$$

**Continuity**

$$\frac{\partial \rho}{\partial t} = - \nabla \cdot (\rho \vec{v}_{tot}) + \nabla \cdot (D_\perp \nabla_\perp \rho) + S_\rho$$

$$\begin{aligned} j &= -R^2 \nabla \phi \cdot \mathbf{J} = \frac{1}{\mu_0} \Delta^* \psi \\ p &= \rho T \end{aligned}$$

**Energy**

$$\rho \frac{\partial p}{\partial t} = - \vec{v}_E \cdot \nabla p - \gamma p \nabla \cdot \vec{v}_E + \nabla \cdot (\kappa_\perp \nabla_\perp T + \kappa_\parallel \nabla_\parallel T) + S_T,$$

# JOREK on HELIOS

**Typical job size:** 20,000 poloidal elements  
5 harmonics  
50 nodes  
~240 hours → ~12,000 node.hours

**Large job size:** 30,000 poloidal elements  
15 harmonics  
150 nodes  
~200 hours → 30,000 node.hours

**XL job size:** 20,000 poloidal elements  
20 harmonics  
~300 nodes  
(short tests)

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- **Physics Results 2015**

  - ELMs**

  - RMP**

  - Pellets**

  - QH-mode**

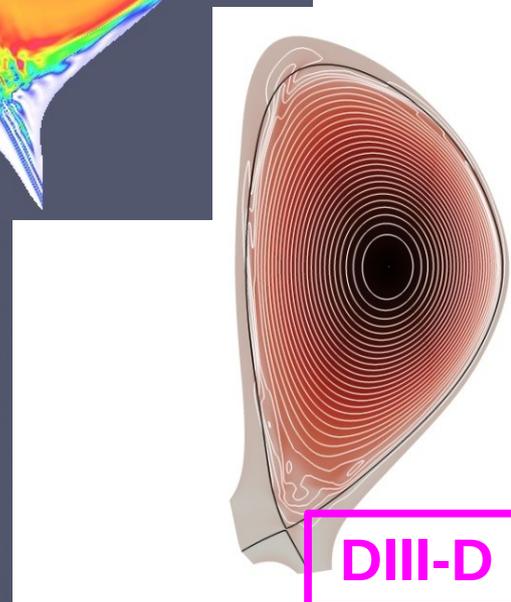
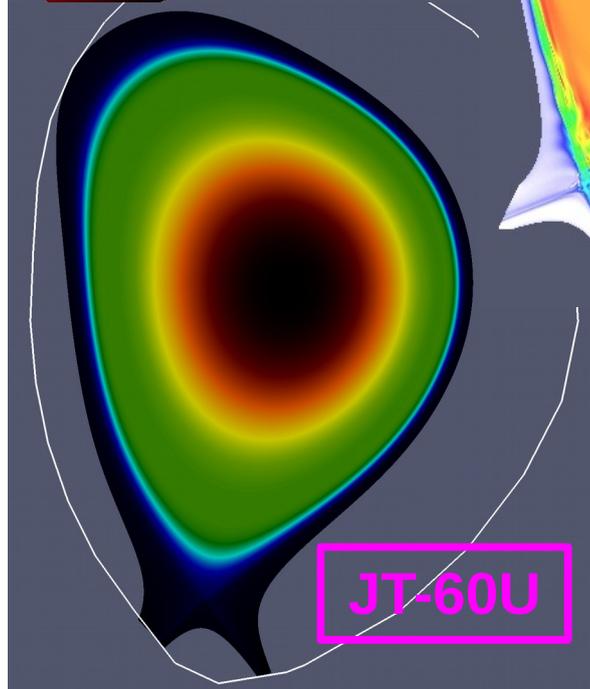
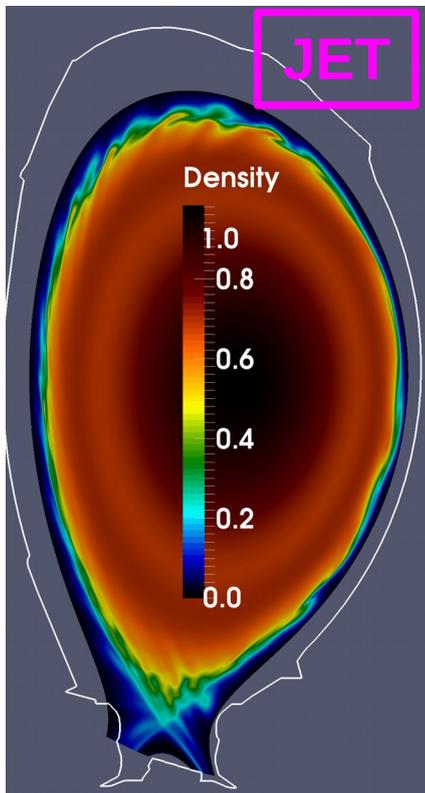
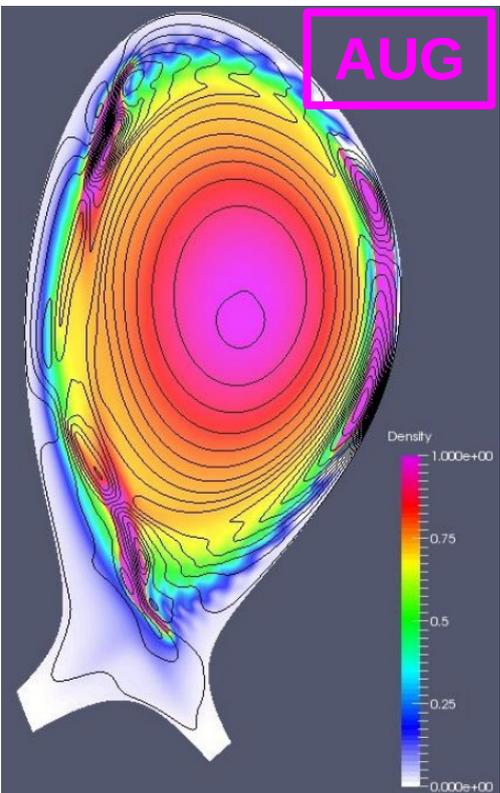
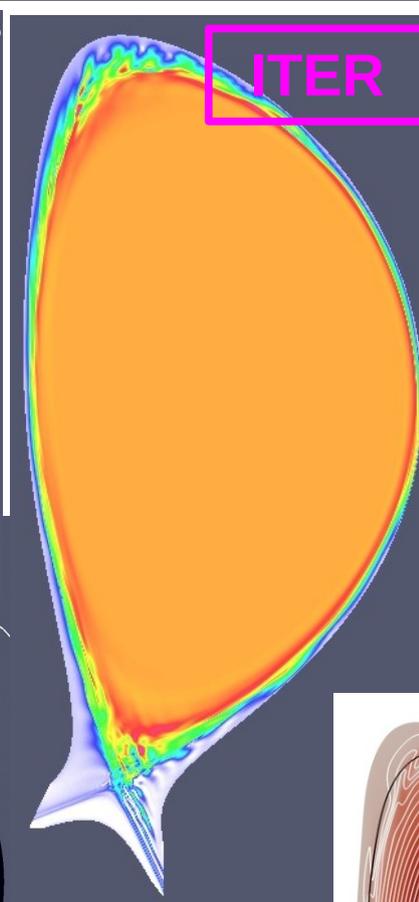
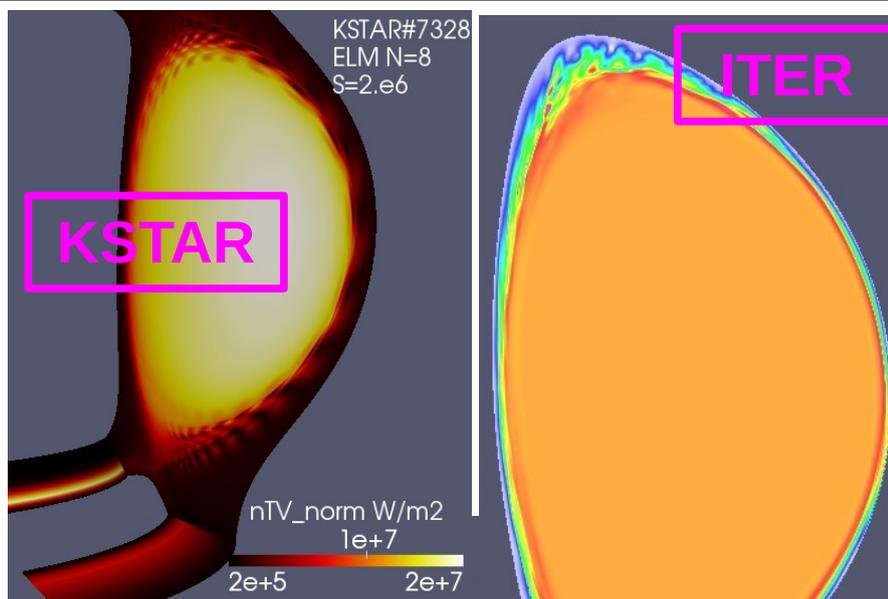
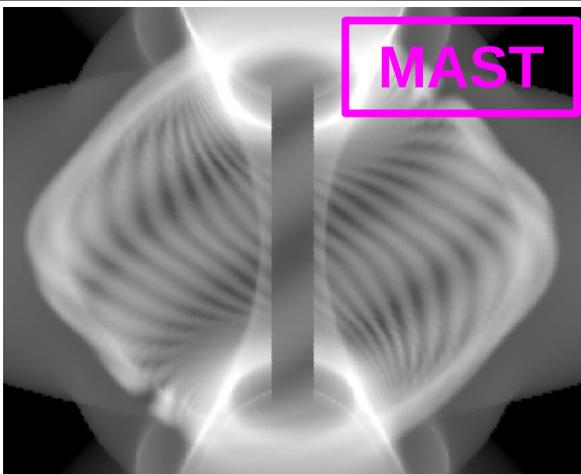
  - MGI disruptions**

- **Conclusion**

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# Devices Simulated



# Edge-Localised-Modes

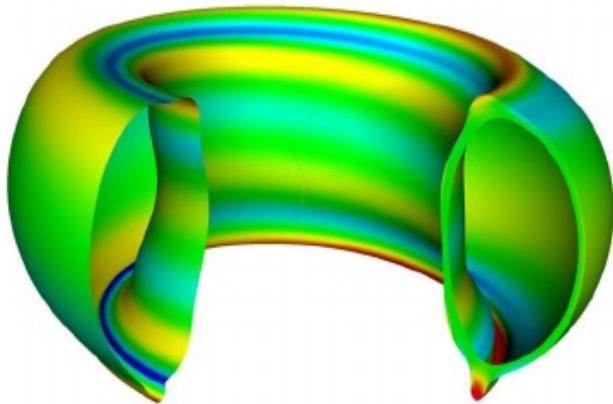
ELMs are necessary for impurity flush-out

But they also need to be controlled due to large divertor heat-fluxes

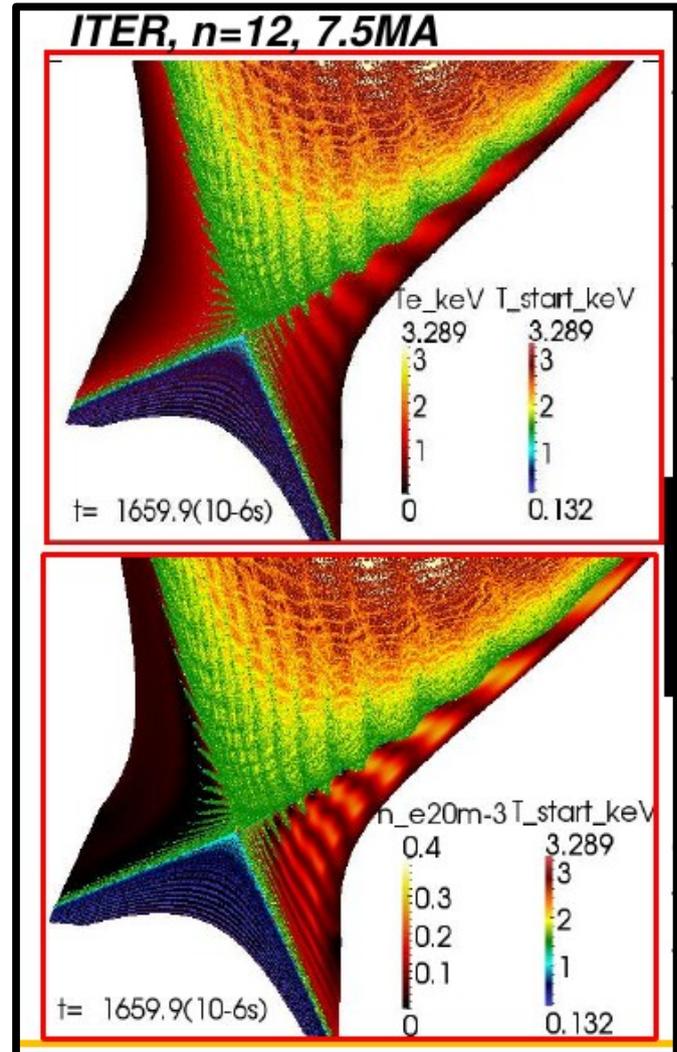
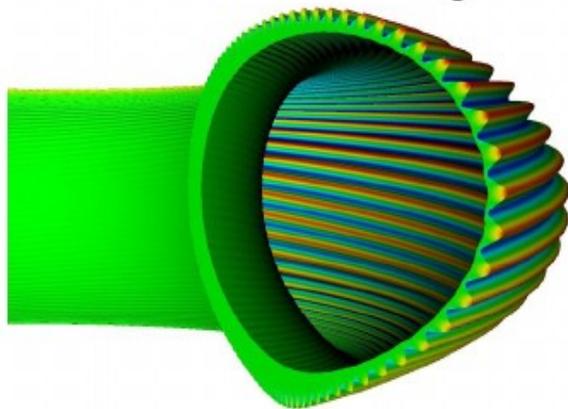
→ Strong need to understand ELMs

Large edge current (bootstrap):  
drives peeling/kink modes

[Huysmans PPCF 2005]



Large edge pressure gradient in  
H-mode drives ballooning modes

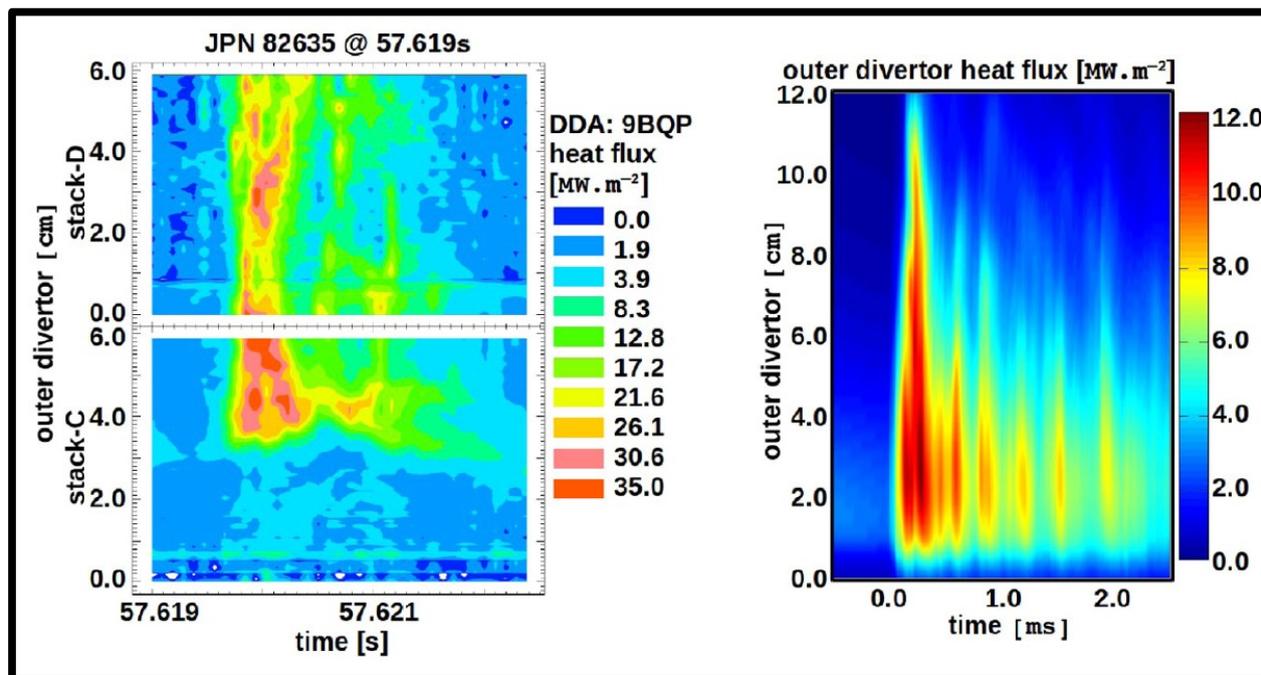


# Validation: Comparison Against Experimental Data

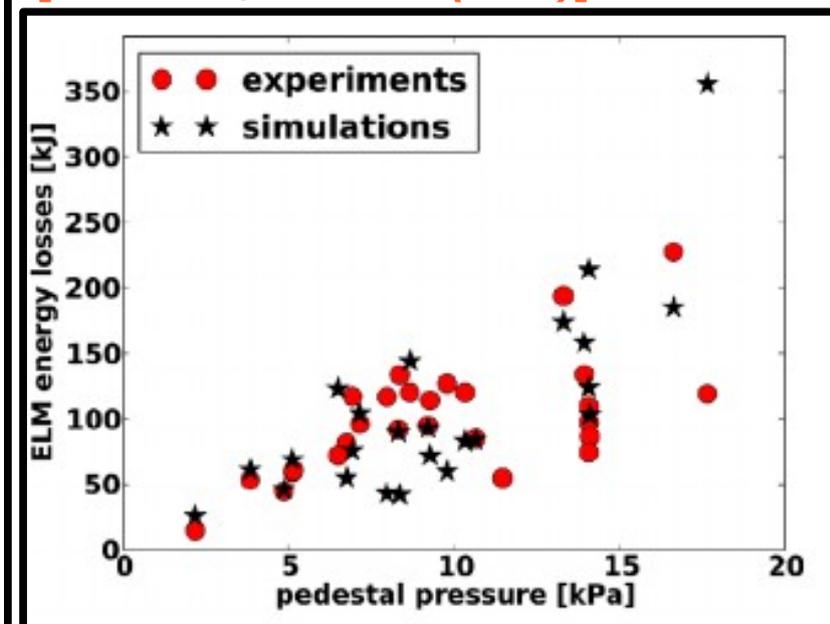
In order to predict ELMs in future devices, simulations must be validated  
→ Quantitative comparison against experimental data

Main comparisons of interest:      ELM energy losses  
   ELM duration  
   Divertor heat-fluxes

Quantitative validation started on JET, to be extended to multi-machines



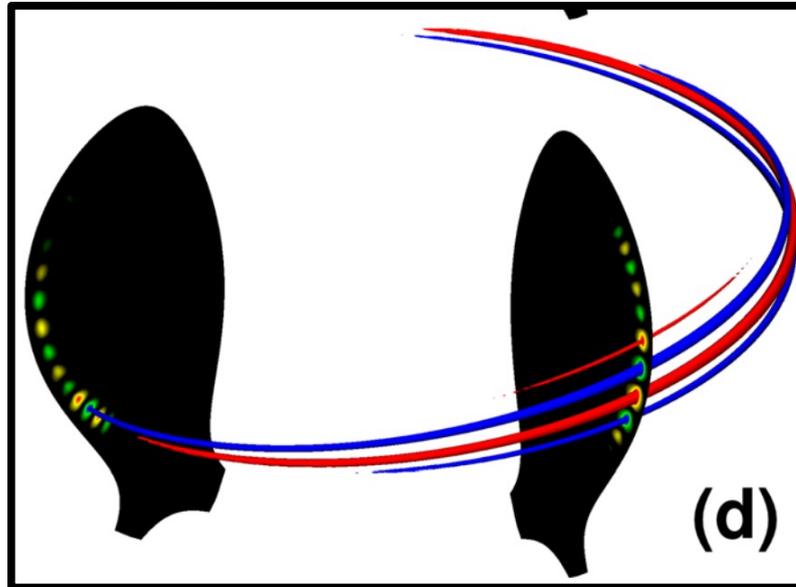
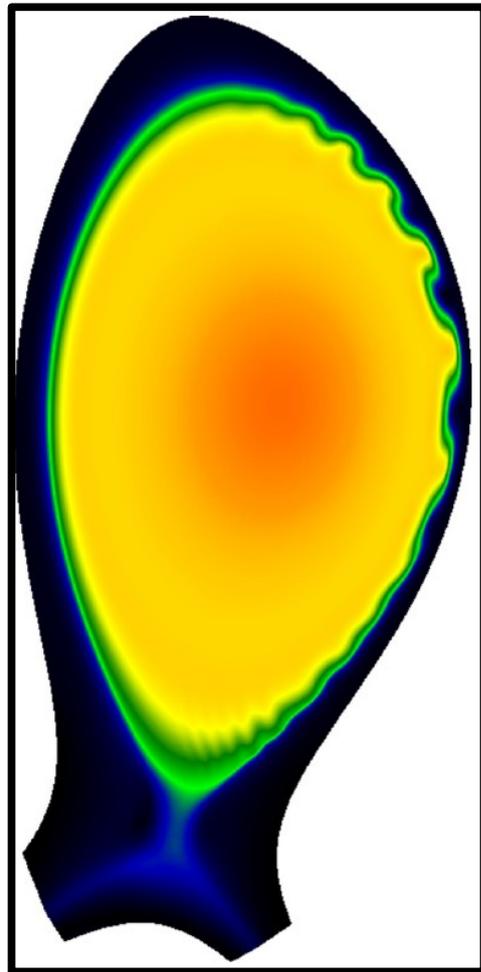
[S.Pamela, *PPCF 58 (2015)*]



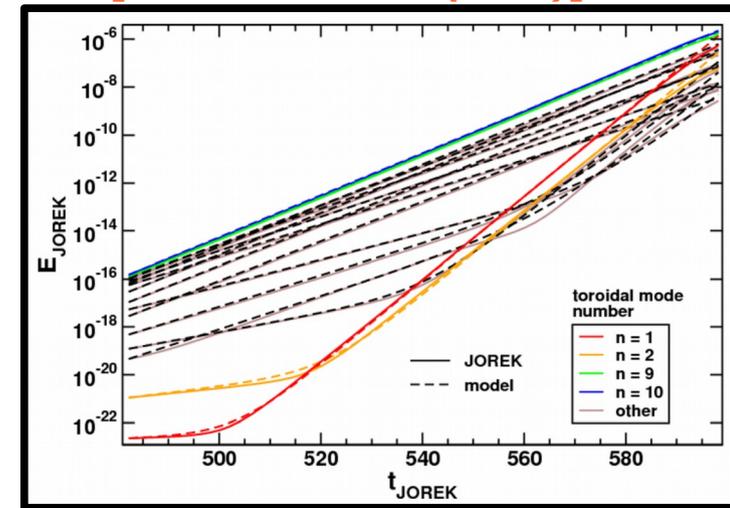
# Toroidal Resolution Required for ELMs

- Large number of toroidal harmonics is important for good ELM representation
- Low mode numbers are linearly sub-dominant, but non-linearly excited
- poloidally and toroidally localised filaments

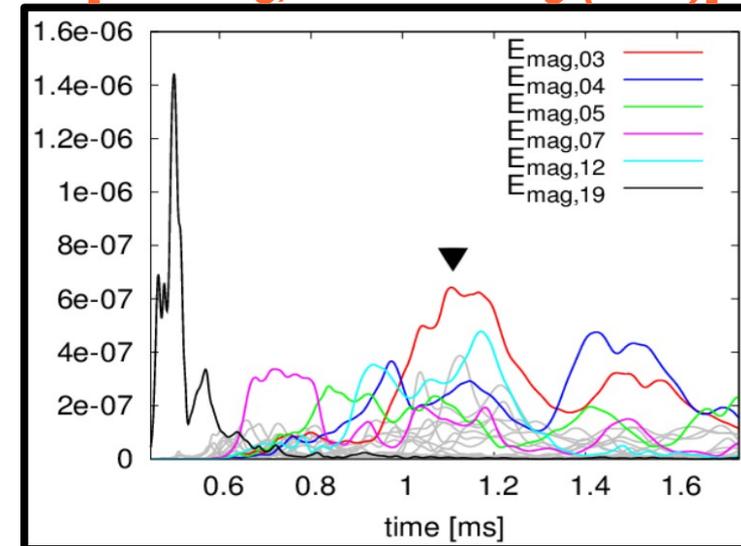
[M.Hoelzl, PoP 19 (2012)]



[I.Krebs, PoP 20 (2013)]



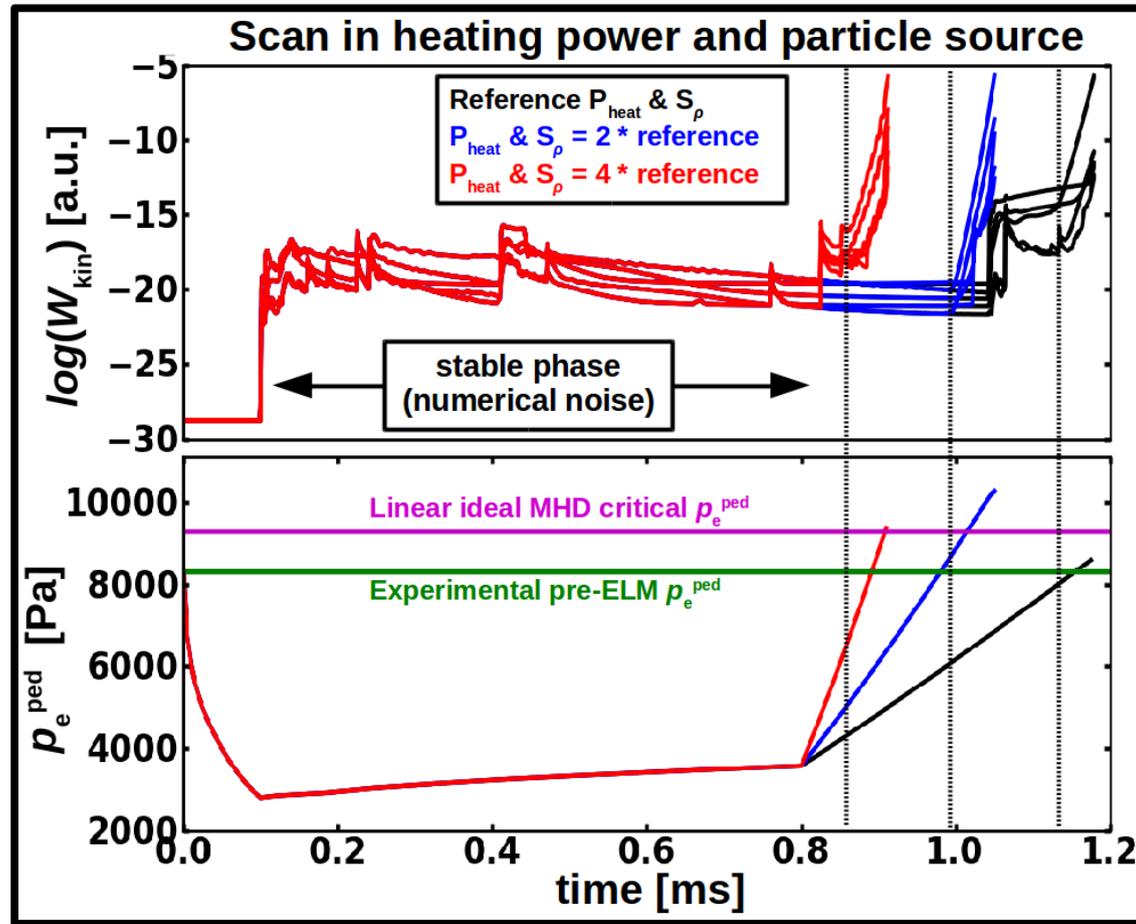
[A.Lessig, DPG meeting (2016)]



# From Validation To Prediction

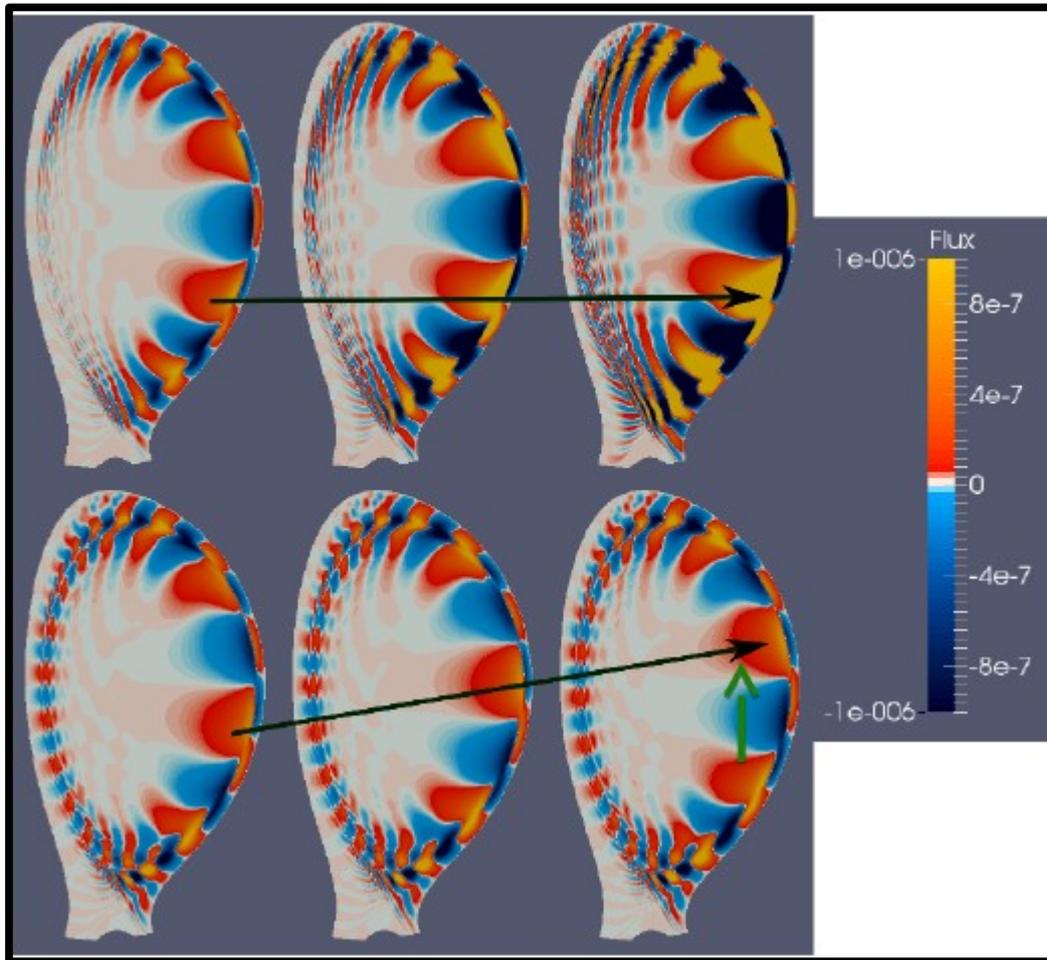
Predictions should include divertor heat-fluxes and ELM energy losses

But also ELM onset information, relevant to pedestal confinement



# The Importance of Diamagnetic Terms

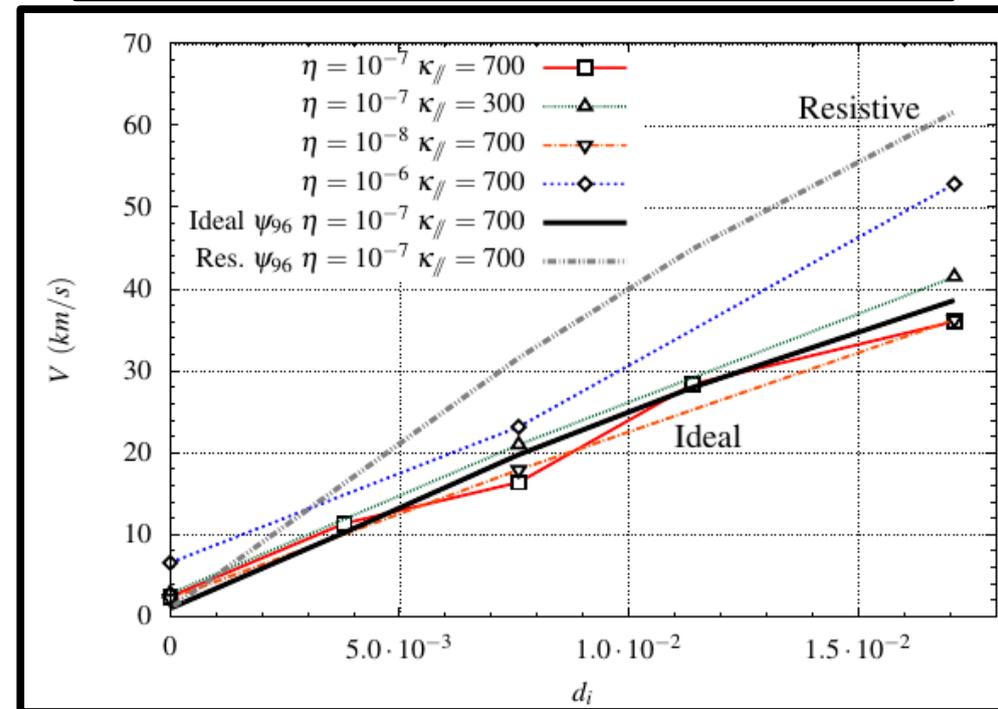
- Diamagnetic effects stabilise high-n mode numbers
- They induce filament rotation
- They enable multiple ELM-cycle simulations



[J.Morales, *subm. PoP (2015)*]

Resistive:  $V_{\text{mode}} = V_{E \times B} + V_{\parallel} \cdot b_{\theta}$

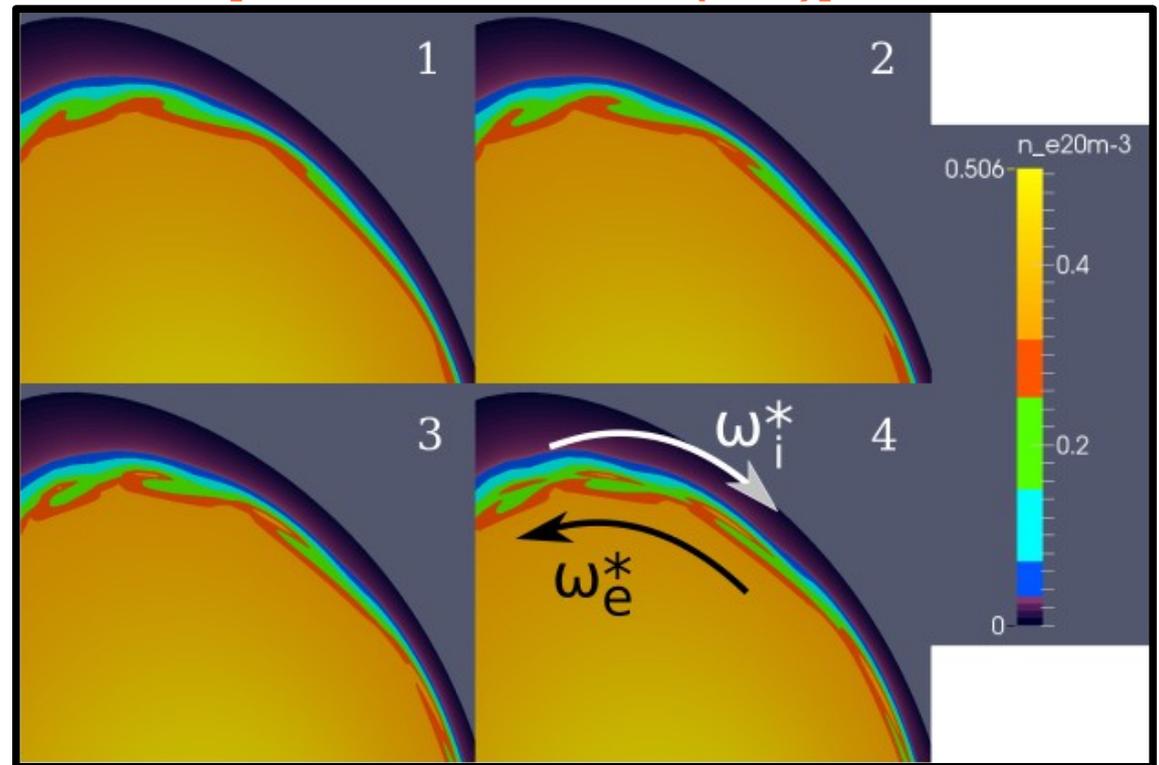
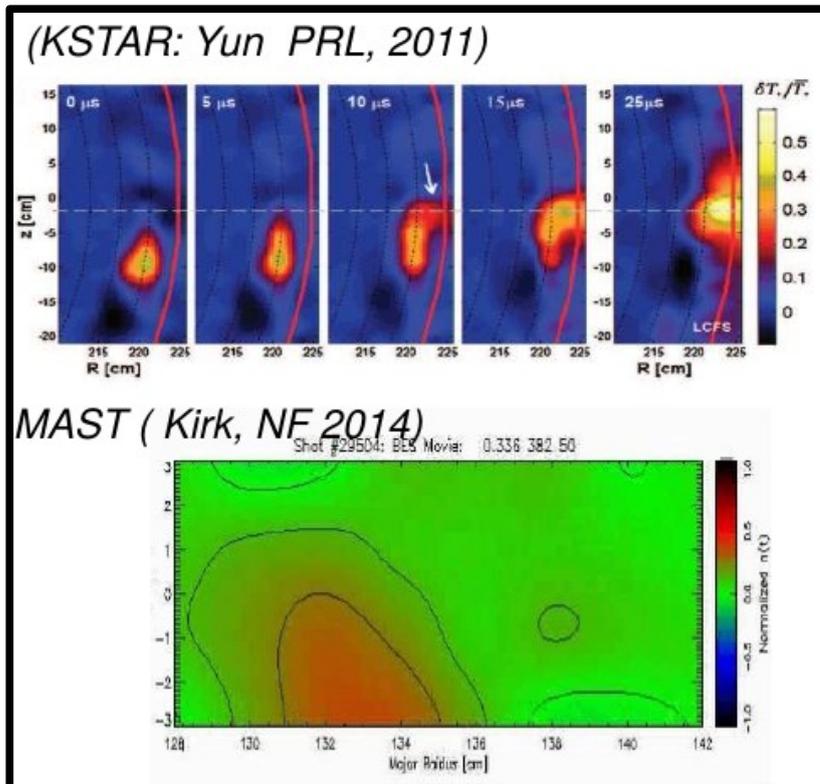
Ideal:  $V_{\text{mode}} = V_{E \times B} + V_{\parallel} \cdot b_{\theta} + V_i^* / 2.$



# Filament Rotation

Filament rotation observed experimentally  
Reproduced by simulations when diamagnetic terms are included  
Filament rotation spreads heat-flux on divertor

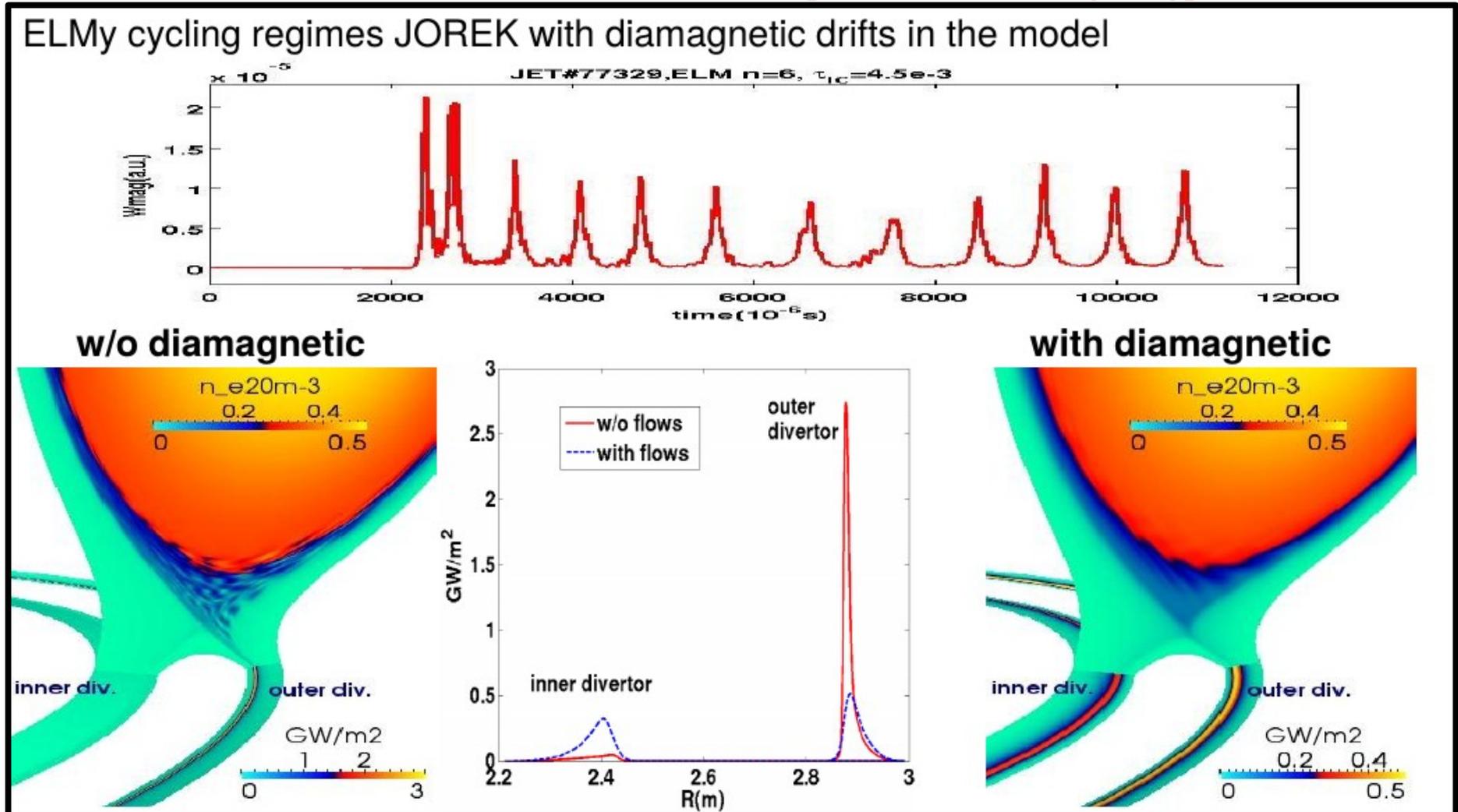
[J.Morales, *subm. PoP (2015)*]



# Diamagnetic Terms & Multiple ELM Cycles

Diamagnetic terms necessary to reproduce multiple ELM cycles  
Necessary to reproduce inner/outer balance of divertor heat fluxes

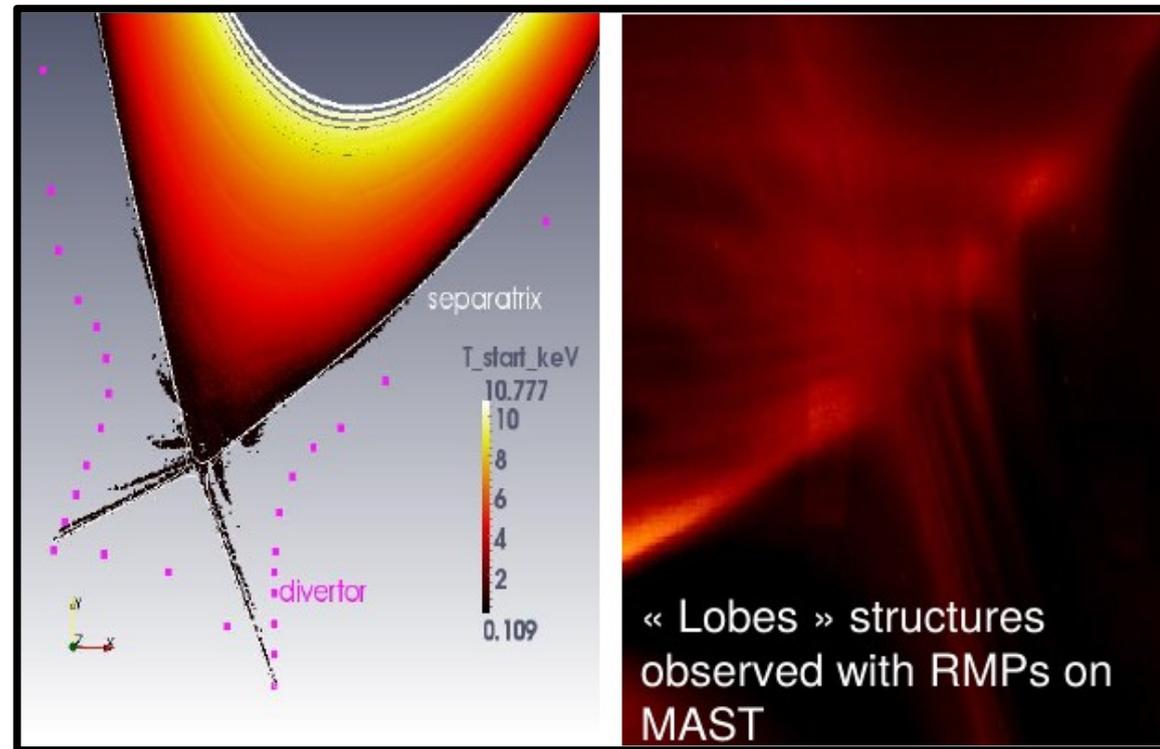
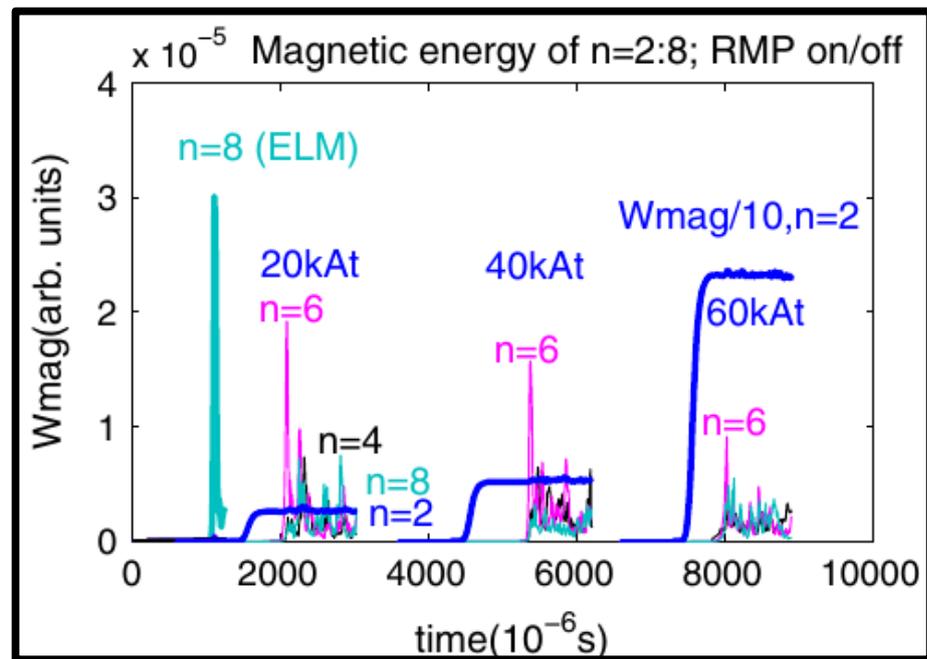
[F.Orain, *PRL* 114 (2015)]



# Mitigation of ELMs by RMPs

RMP simulations reproduce the mitigation of ELMs  
Lobes observed near the X-point, like in MAST experiments

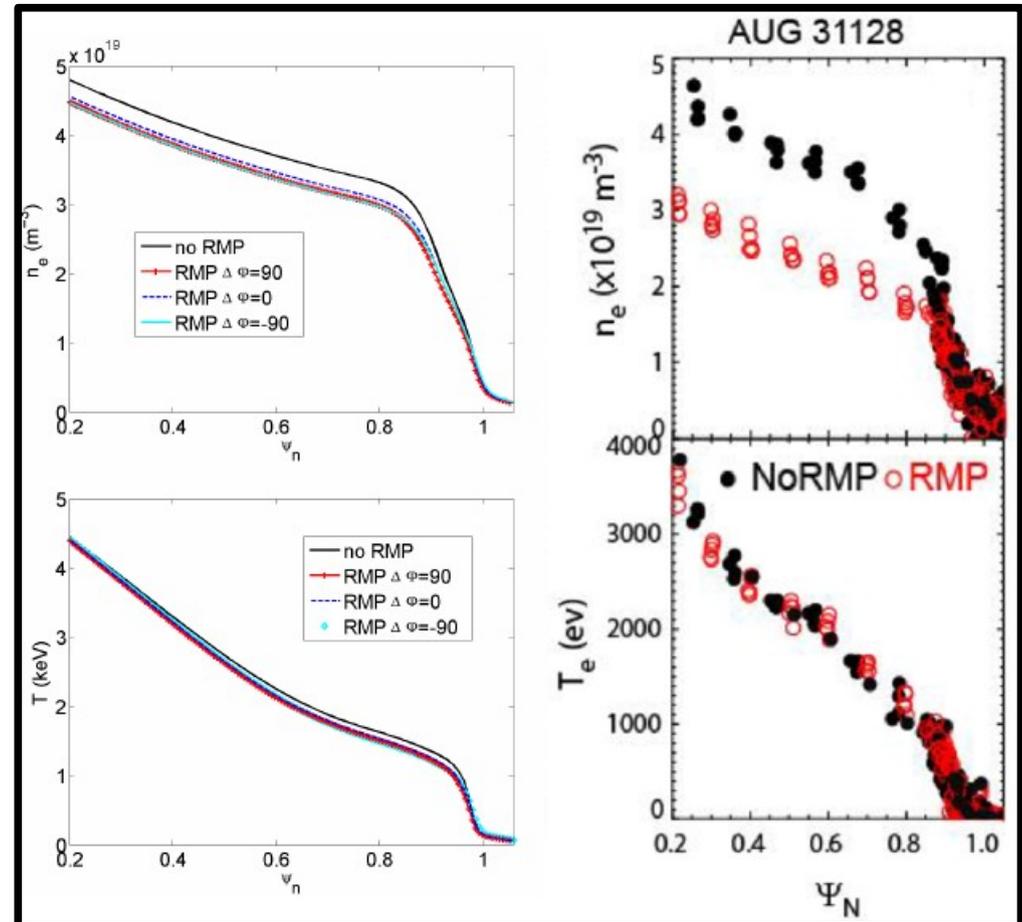
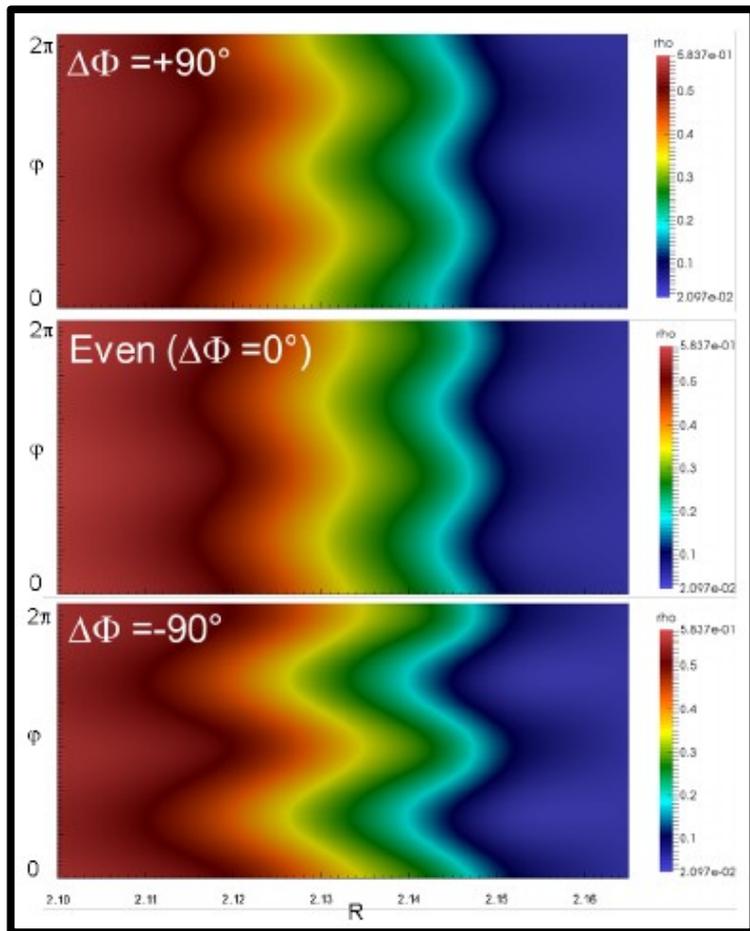
[M.Becoulet, *PRL* 113 (2014)]



# Mitigation of ELMs by RMPs

- Simulation of density pump-out are progressing
- Mitigation more efficient if applied perturbation is amplified by excitation of modes at plasma edge
  - larger corrugation at X-point
  - larger lobes
  - larger pump-out

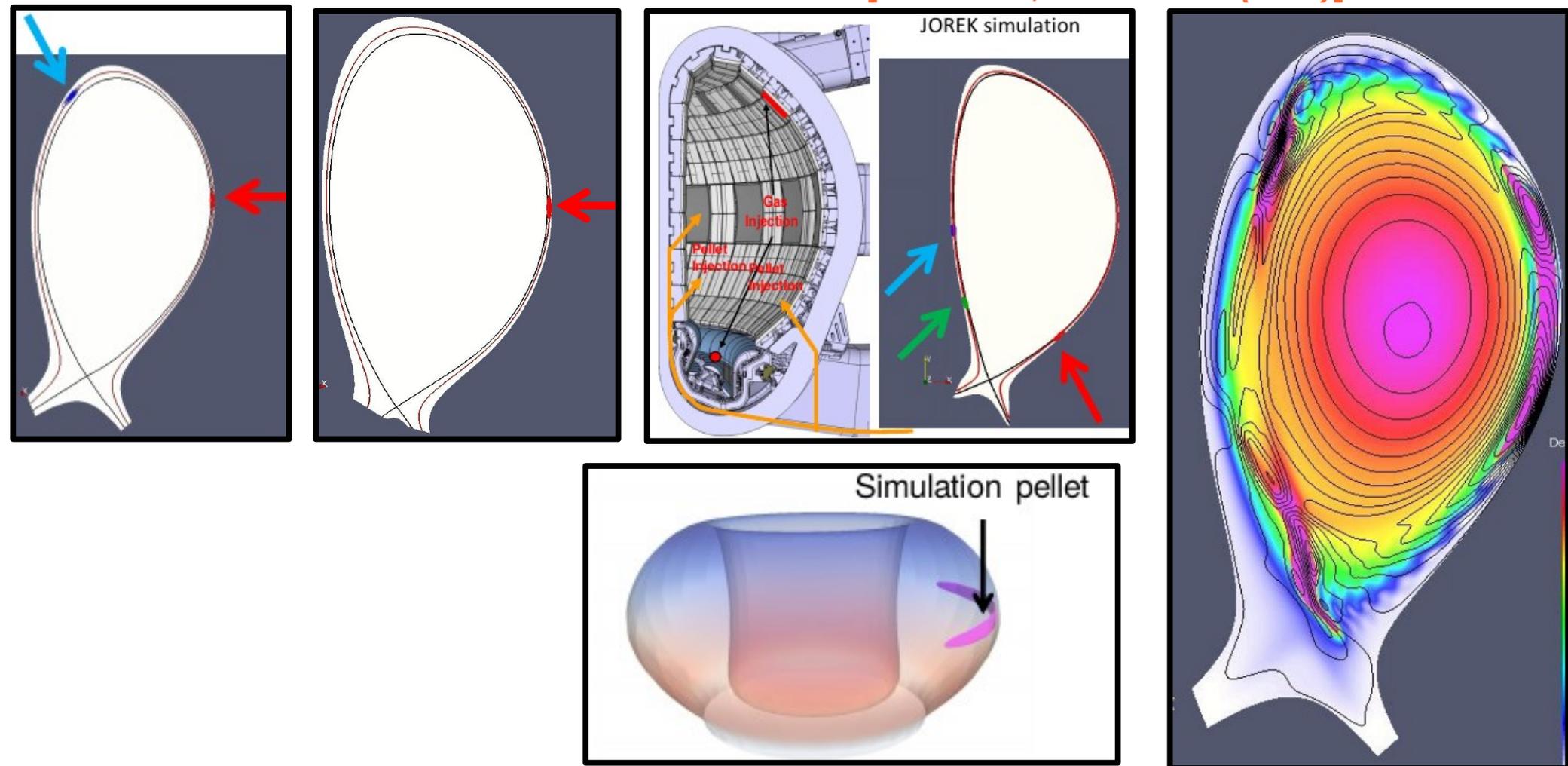
[F.Orain, *subm. Nucl.Fus.* (2016)]



# Pellet-Triggered ELMs

Simulations done on several devices, using various pellet injection locations  
Pellet ablates as it enters the plasma, density cloud propagates along flux tube  
Ballooning modes are excited, and ELM is triggered

[S.Futatani, *Nuc.Fus.* 54 (2014)]



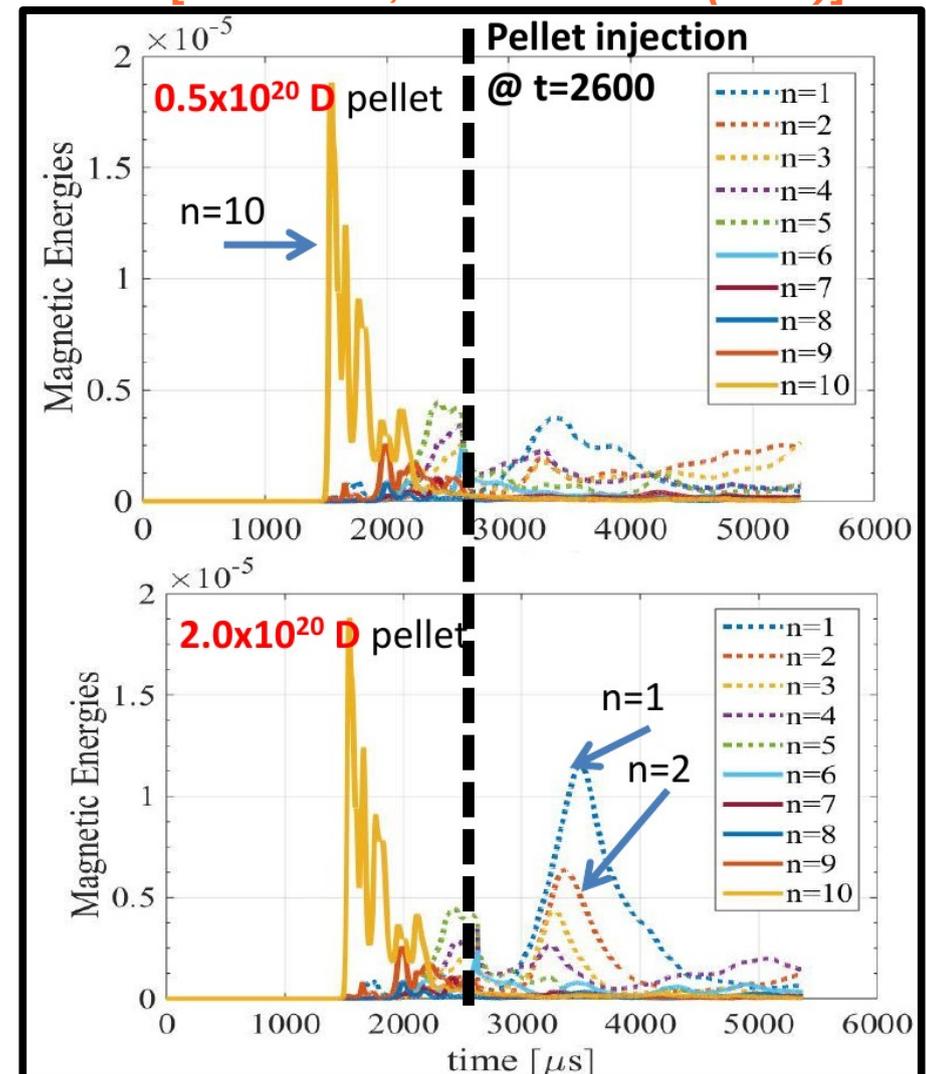
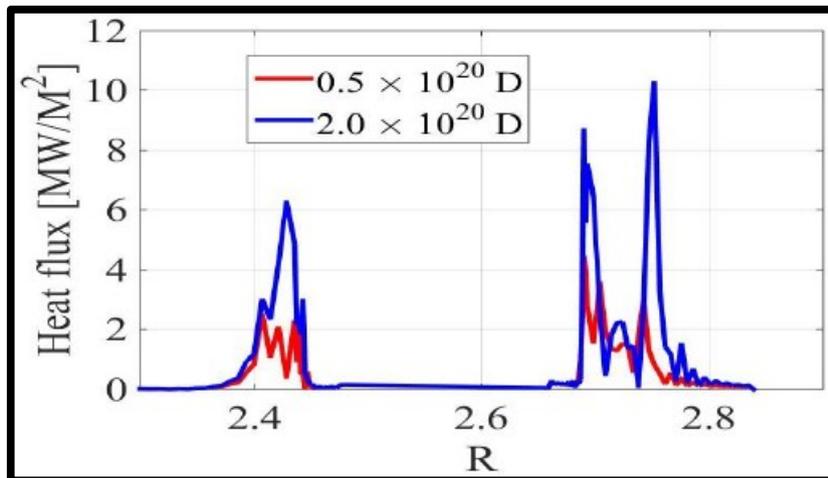
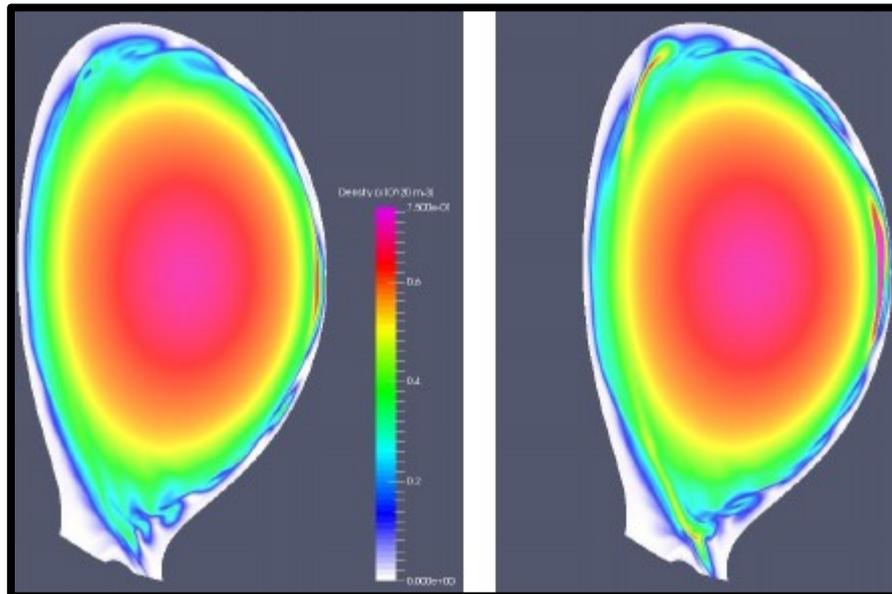
# Pellets (2)

Simulations for small and large pellets on JET

ELM clearly triggered by large pellet.

Divertor heat flux is split (also observed experimentally)

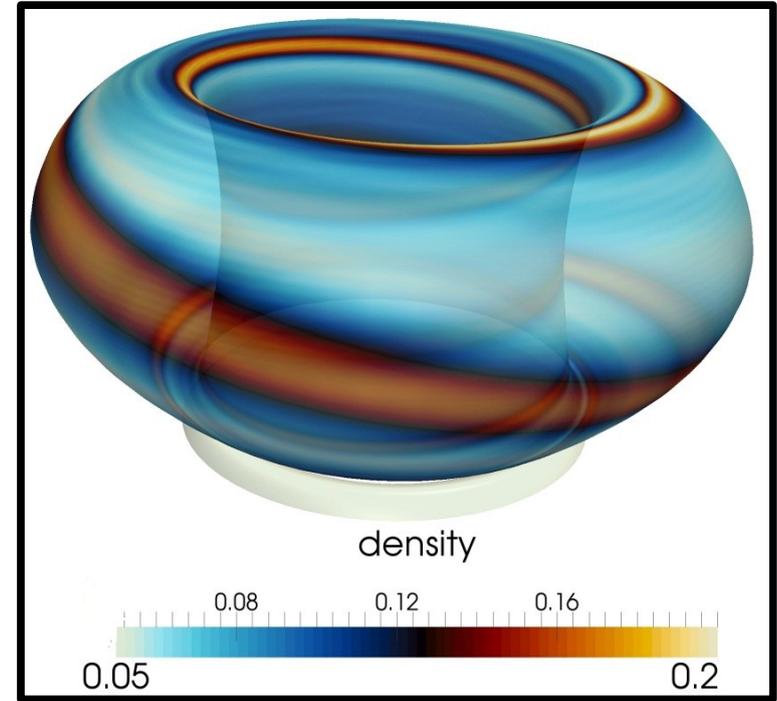
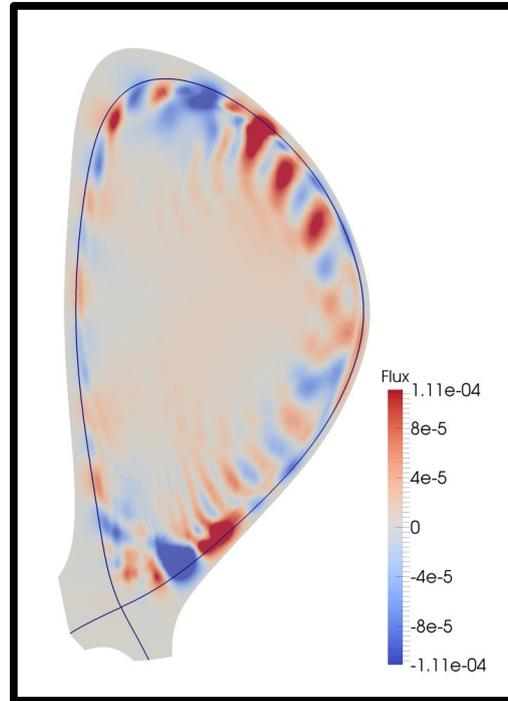
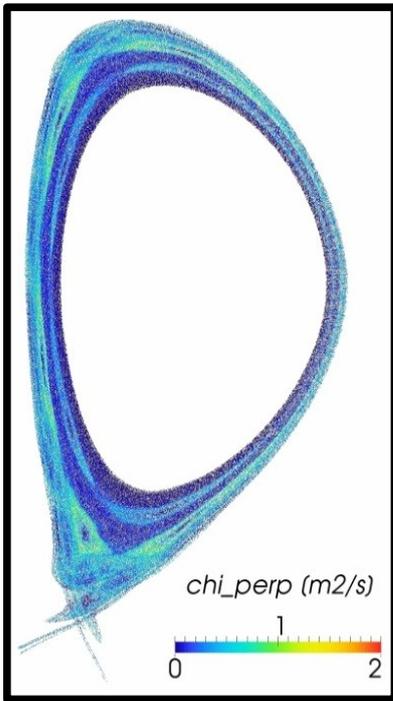
[S.Futatani, recent results (2016)]



# QH-mode Simulations

- QH-mode simulations for DIII-D
- Saturated kink-peeling mode at the plasma edge
- Edge Harmonic Oscillation (EHO) causes density losses
- Rotation frequency agrees with experiments
- $n=1$  dominant mode

[F.Liu, *Nuc.Fus* 55 (2015)]



# Mitigation of Disruptions with MGI

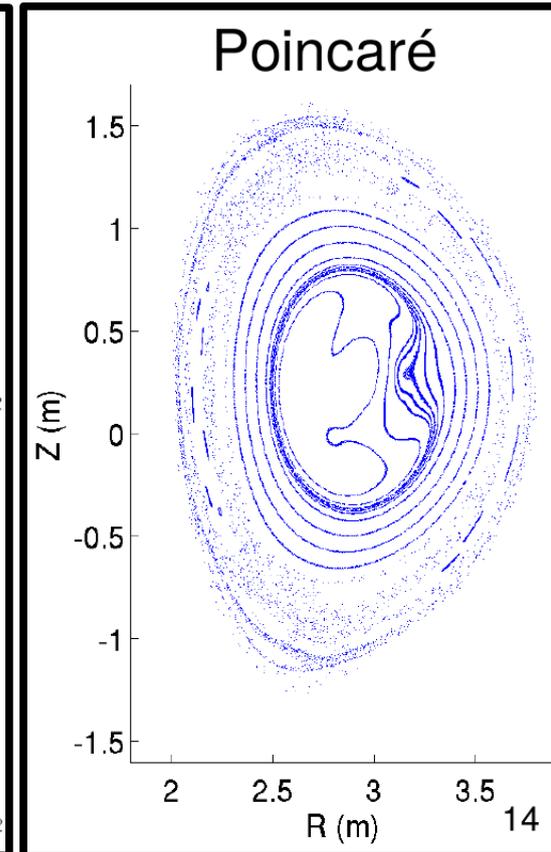
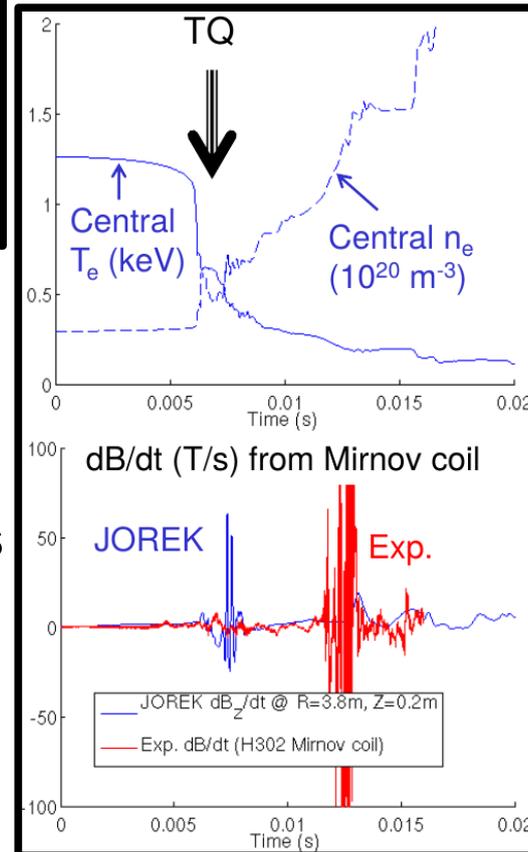
$$\text{Energy: } \frac{\partial(\rho T)}{\partial t} = -\mathbf{v} \cdot \nabla(\rho T) - \gamma \rho T (\nabla \cdot \mathbf{v}) + \nabla \cdot (\kappa_{\perp} \nabla_{\perp} T + \kappa_{\parallel} \nabla_{\parallel} T) + \frac{2}{3R^2} \eta_{\text{Spitzer}} j^2 - \xi_{\text{ion}} \rho \rho_n R_{\text{ion}}(T) - \rho \rho_n L_{\text{rays}}(T) - \rho^2 L_{\text{brem}}(T)$$

$$\text{Neutral density: } \frac{\partial \rho_n}{\partial t} = \nabla \cdot (D_n : \nabla \rho_n) - \rho \rho_n R_{\text{ion}}(T) + \rho^2 R_{\text{rec}}(T) + S_n$$

- Neutrals are deposited via a **volumetric source term**
- Neutral transport is diffusive
- **ionization, recombination** and **radiation** (line and bremsstrahlung) with coefficients from the ADAS database
- **Ohmic heating** (with Spitzer resistivity)

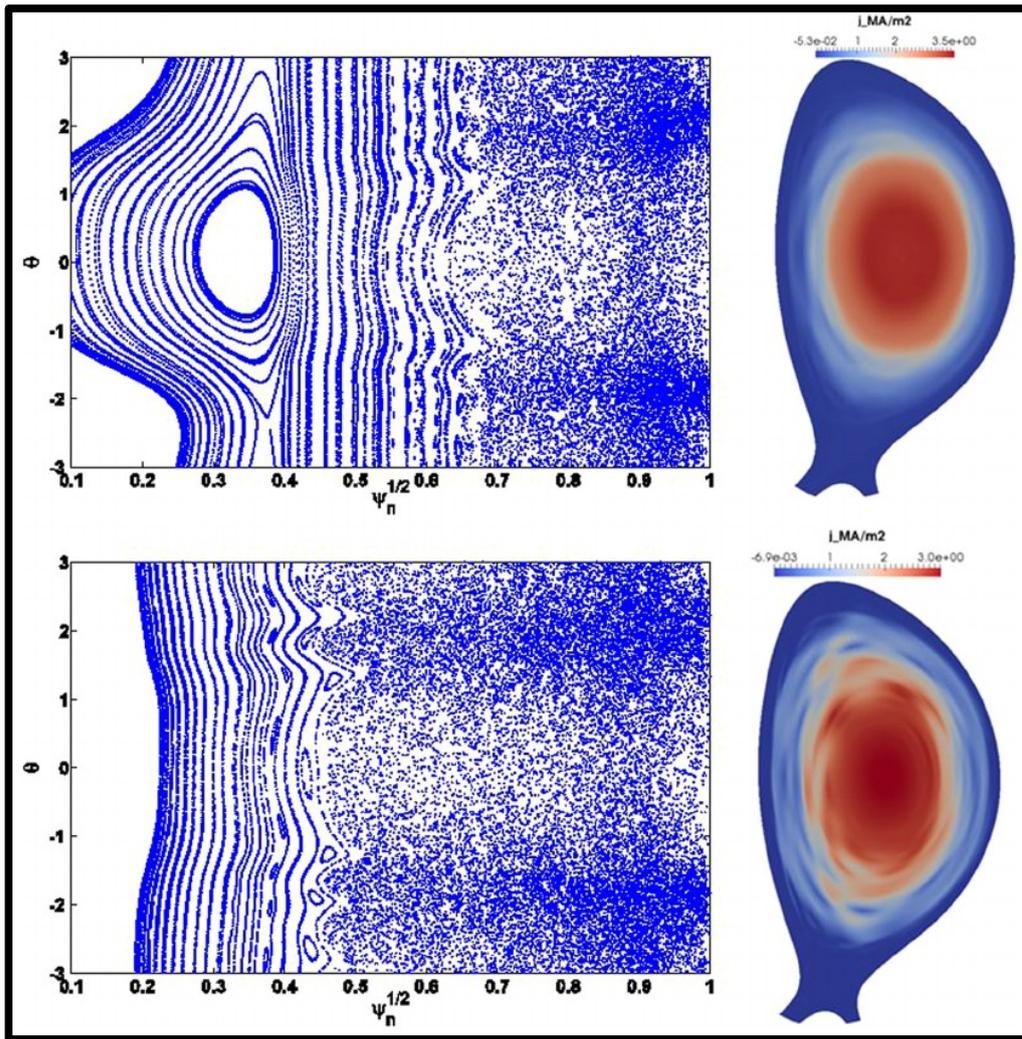
[A.Fil, *PoP* 22 (2015)]

- MGI using neutral density model
- Tearing modes and internal kink leads to thermal quench
- Cooling by parallel conduction along ergodic field lines

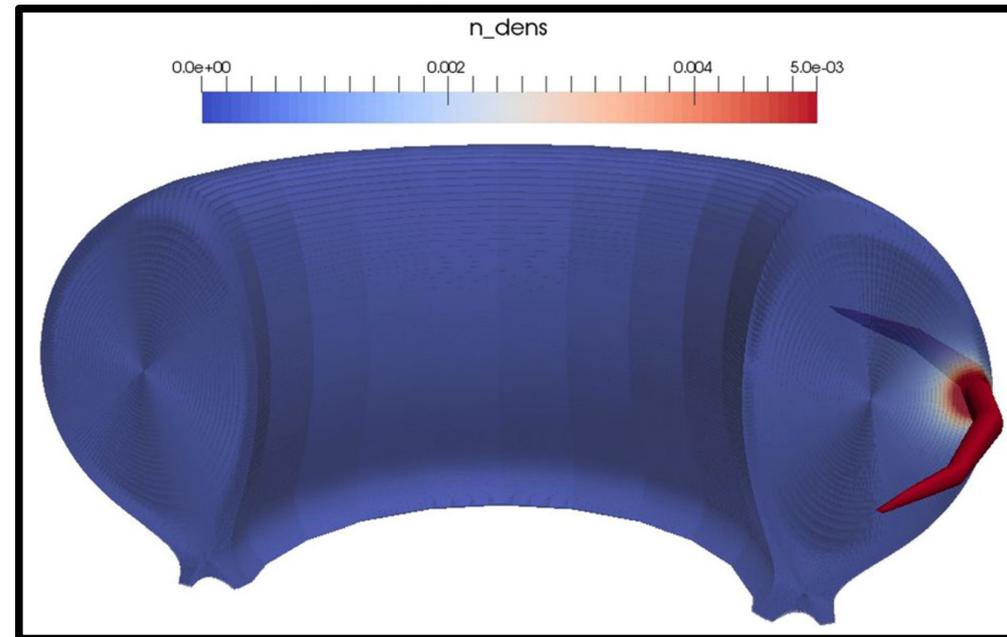


# Mitigation of Disruptions with MGI

- More work needed to push resistivity closer to experimental values  
→ try to match agreement with magnetic probes



[A.Fil, *PoP* 22 (2015)]

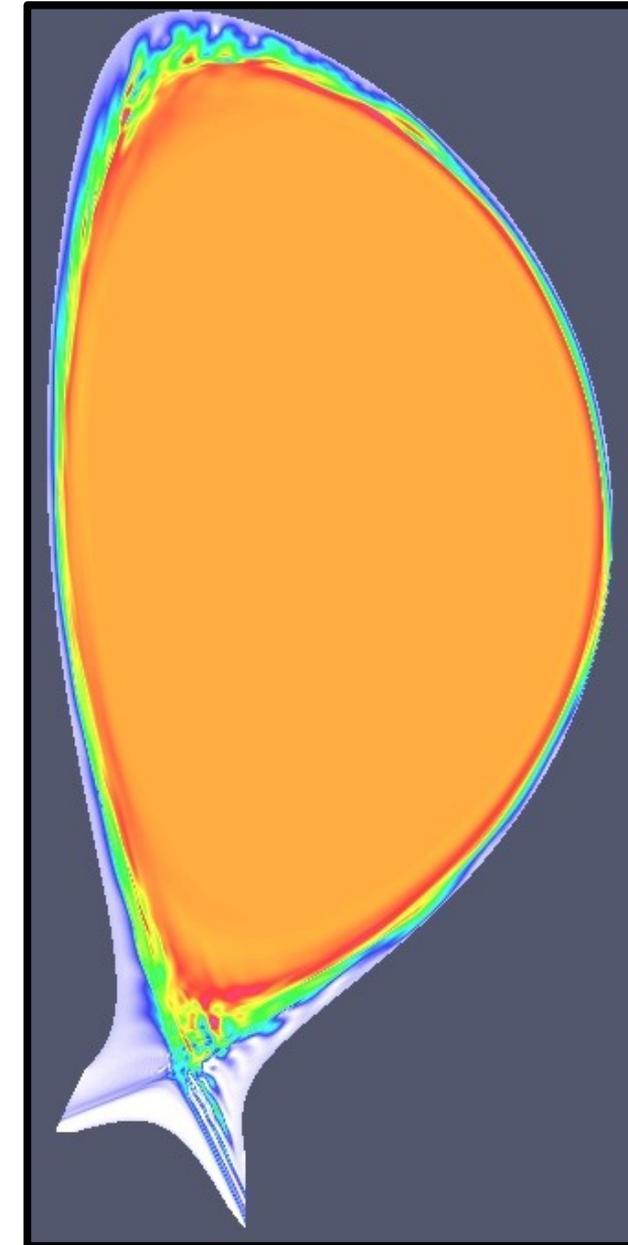
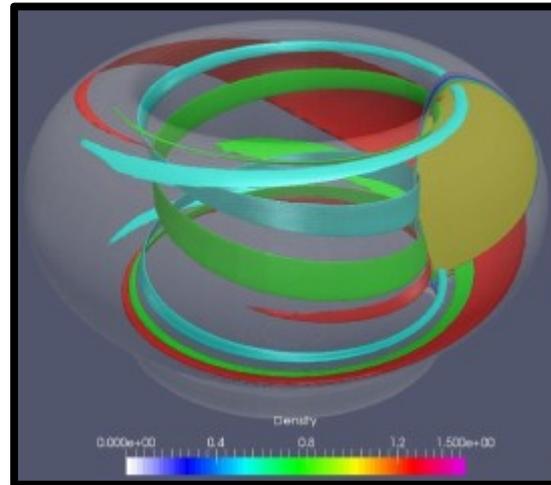
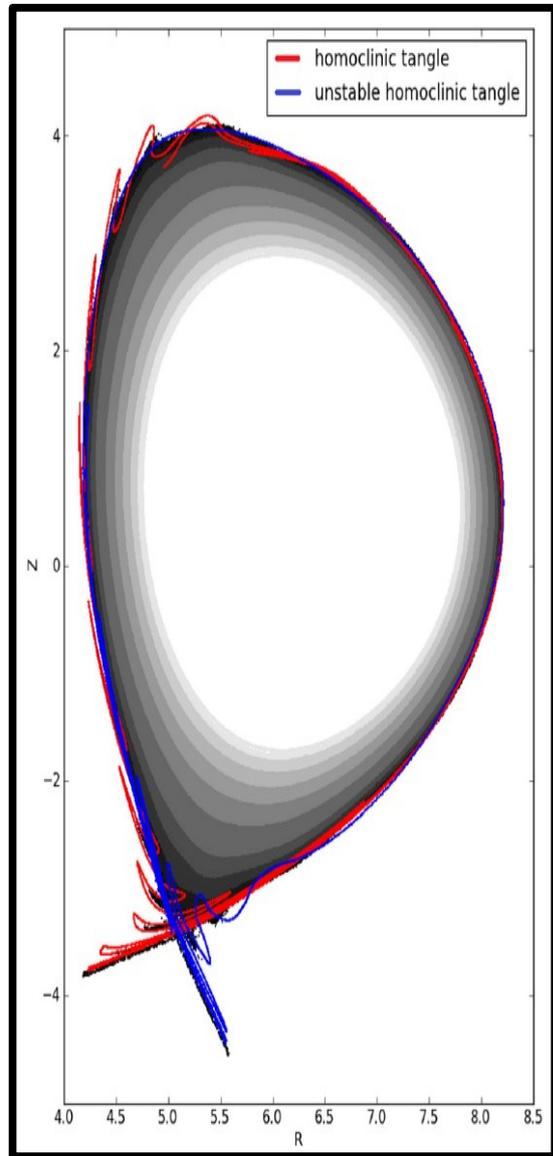


# ITER Simulations

[F.Orain, *PoP* 20 (2013)]

ITER simulations of ELMs, RMPs and pellets published.

[S.Futatani, *Nuc.Fus.* 54 (2014)]



# Summary

- Please visit [www.jorek.eu](http://www.jorek.eu) !
- Large JOREK team across Europe
- Eurofusion ENR project is progressing well
- ELMs simulation close to quantitative validation
- Now working on multiple type-I ELM cycles
- Mitigation of ELMs by RMPs is coming closer to experiments
- Pellet-triggered ELM simulations already achieved on many devices
- First non-linear QH-mode simulations show good agreement with DIIID
- MGI disruptions have successfully reproduced thermal quench

# Acknowledgments

---

**THANK YOU!**

**Many Thanks to the CSC-team  
on behalf of all HELIOS users.**

**HELIOS has enabled the JOREK  
team to obtain many important  
results in the last years!**

# References/Acknowledgements

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